

COMP225 MID SEMESTER TEST (3 QUESTIONS, 20 MARKS)

1. (5 marks) Consider the definition of a node for binary trees.

```
struct treeNode {
    int item;
    treeNode* LChildPtr;
    treeNode* RChildPtr;
};
```

```
typedef treeNode* ptrType;
```

- (a) (3 marks) Write a program to compute the maximum value in a binary tree t . You may return -1 for NULL trees.

```
int maxVal (treeNode t);
// POST: returns the maximum value in the tree t
```

- (b) (2 marks) What is the worst case complexity of your program for a tree with n nodes? Sketch a diagram of a tree which has this worst-case behaviour.

2. (5 marks)

- (a) (3 marks) Write a program to compute the product of all items in a binary tree, having values strictly greater than a and no more than b . You may return 1 for NULL trees.

```
int productBetween (treeNode t, int a, int b);
//PRE: a <= b
//POST: returns the sum of the items in t with values v, such that a < v <= b
```

- (b) (2 marks) What is the worst-case complexity of your program, for trees with n nodes. Does the complexity depend on the shape of the tree. State your reasons.

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3. (10 marks) This question is about dynamic programming. Consider the following problem for finding the *longest strictly increasing subsequence*. Given an array A of length n having integer values, determine a subsequence (not necessarily contiguous) of maximum length in which the values in the subsequence form a strictly increasing sequence. (Recall that a subsequence of an array is obtained by “crossing out” elements.)

For example if the array is $[2, 4, 2, 8, 1, 2]$ then the longest strictly increasing subsequence has length 3, and it is $[2, 4, 8]$.

The following program partially solves this problem. Given an array A of length n and an index j , it computes the longest strictly increasing subsequence in $A[0..j]$ which includes the item $A[j]$.

```
int subseq (int A[], int n, int j) {
    int m;
    if (j==0) return 1;
    else {
        m= 1;
        for (int i= 0; i < j; i++)
        {
            if (A[i] < A[j]) { int x= subseq(A, n, i);
                if (x + 1 > m) {m= x + 1;}
            }
        }
    }
    return m;
}
```

For example `subseq(A, 6, 2)` returns 1 because the longest increasing subsequence in $A[0..2]$ which must include $A[2]$ is $[2]$. However `subseq(A, 6, 3)` returns 3, because the longest increasing subsequence in $A[0..3]$ which must include $A[3]$ is $[2, 4, 8]$.

- (a) (5 marks) The above program does not use a look-up table to store previously computed values. Rewrite the program so that it does. Use the following template.

```
int subseqDP (int A[], int n, int j, int LookUp[]);
```

and use the definition of `subseq` as a basis. In your solution only make the following changes: change one of the `if` statements, add an update to `LookUp` and, in the recursive call, change the name.

- (b) (5 marks) Describe how you would use `subseqDP` to solve the *longest strictly increasing subsequence* problem.